

constant acceleration motion

$$d = \frac{1}{2}(v_f + v_i)t \quad d = v_0t + \frac{1}{2}at^2 \quad v_f = v_i + at \quad v_f^2 = v_i^2 + 2ad$$

projectile motion  $x = x_0 + v_0t \cos \theta_i$   $y = y_0 + v_0t \sin \theta_i - (1/2)gt^2$ 

$$\text{max height} = \frac{(v_0 \sin \alpha)^2}{2g} \quad \text{flight time} = \frac{2v_0 \sin \alpha}{g} \quad \text{range} = \frac{v_0^2 \sin 2\alpha}{g}$$

work  $W = \mathbf{F} \cdot \mathbf{d} = \int_{x_i}^{x_f} \mathbf{F} dx = \Delta KE = P \cdot t = -\Delta U = (1/2)kx^2$ 

$$W_{\text{you}} = \Delta U_{\text{field}} = -W_{\text{field}}$$

potential energy (conservative work)

$$\Delta U = mg\Delta h \quad U_{\text{spring}} = (1/2)k(x_f - x_0)^2 \quad \frac{dU}{dx} = -F_x \quad F_x = -kx$$

conservation of energy

$$K_i + U_i = K_f + U_f \quad \Delta KE = W \quad KE_{\text{total}} + U_{\text{total}} = E_{\text{total mech}}$$

 $W = \Delta E_{\text{mech}} + \Delta E_{\text{th}}$  - to keep track of non-conservative forcespower  $P = \frac{dW}{dt} = \mathbf{F} \cdot \mathbf{v} = \tau\omega$  non-constant acceleration  $Pt = (1/2)mv^2$   $P = \tau\omega$ center of mass  $\frac{\sum m_i \mathbf{r}_i}{M}$   $I' = I_{cm} + Md^2$ , d is distance from c.o.m.inertia  $I = \sum_i m_i r_i^2$   $I = \int r^2 dm$ linear momentum  $\mathbf{p} = m\mathbf{v}$ impulse  $\mathbf{I} = \int \mathbf{F} dt = \Delta \mathbf{p}$ newton's 2<sup>nd</sup> law  $\mathbf{F}_{\text{net}} = d\mathbf{p} / dt$ average force  $\mathbf{F}_{\text{ave}} = 1/\Delta t \int \mathbf{F} dt = \mathbf{I} / \Delta t$ 

rotational motion

angular displacement  $\theta$  spatial displacement  $x = \theta r$ angular velocity  $\omega = \frac{d\theta}{dt}$  spatial velocity  $v = \omega r$ angular acceleration  $\alpha = \frac{d\omega}{dt}$  spatial linear acc.  $a = \alpha r$ spatial centr. acc.  $v^2 / r = \omega^2 r$ 

torque

$$\tau = \mathbf{r} \times \mathbf{F} = I\alpha = rF \sin \theta = r_{\perp} F = \frac{d\mathbf{L}}{dt}$$

angular momentum

$$\mathbf{L} = \mathbf{r} \times \mathbf{p} = I\omega = m(\mathbf{r} \times \mathbf{v}) = rp \sin \theta$$

angular impulse

$$\Delta \mathbf{L} = \int \tau dt$$

gravity

$$\mathbf{F}_{1,2} = -\frac{Gm_1 m_2}{r_{1,2}^2} \mathbf{r}_{1,2} \quad \mathbf{F} = -\frac{Gm_1 m_2}{r^2} \quad U(r) = -\frac{Gm_1 m_2}{r} \quad E = \frac{1}{2}mv^2 - \frac{GMm}{r}$$

simple harmonic motion

$$ma_x = -kx \quad \ddot{x} - \frac{k}{m}x = 0$$

waves

$$x = A \cos(\omega t + \phi)$$

$$v = -\omega A \sin(\omega t + \phi)$$

$$a = -\omega^2 A \cos(\omega t + \phi) = -\omega^2 x$$

$$y(x, t) = A \cos\left(\frac{2\pi}{\lambda}(x - vt)\right)$$

$$y(x, t) = A \cos(kx - \omega t)$$

traveling wave to the right

$$K = \frac{1}{2}kA^2 \sin^2(\omega t + \phi)$$

$$U = \frac{1}{2}kA^2 \cos^2(\omega t + \phi)$$

$$E = \frac{1}{2}kA^2$$

$$T = \frac{1}{f} = \frac{2\pi}{\omega} = \frac{2\pi}{\sqrt{k/m}}$$

simple pend.  $T = 2\pi \sqrt{\frac{l}{g}}$

$$I\alpha = -mgL \sin \theta$$

$$\omega = \sqrt{k/m}$$

physical  $T = 2\pi \sqrt{\frac{I_{total}}{M_{total}gd_{c.o.m.}}}$

$$I\alpha = -mgh \sin \theta$$

$$v = \sqrt{T/\mu}$$

speed of wave on string

$$v = \lambda/T = \omega/k$$

just the vibrations

$$k = 2\pi/\lambda$$

angular wave number

$$\phi = 1/2 \mu \omega^2 A^2 v \quad \mu = \Delta m / \Delta x$$

Elastic Modulus = stress/strain | stress = force per unit area | strain = degree of dermation | stress is proportional to strain with a k, elastic modulus.

$$Y = \frac{F/A}{\Delta L/L_i} \quad S = \frac{F/A}{\Delta x/h} \quad B = \frac{\Delta F/A}{\Delta V/V_i} \quad \text{Young, Sheer, Bulk}$$

$$A_1 v_1 = A_2 v_2 \quad \text{fluid}$$

$$FA = FA \quad \text{fluid}$$

$$P + 1/2 \rho v^2 + \rho g y = \text{constant}$$

$$v = \sqrt{B/\rho} \quad \text{speed of sound wave} \quad B = \text{Bulk Modulus}$$

$$\Delta P = \Delta P_{\max} \sin(kx - \omega t) \quad \Delta P_{\max} = \rho v \omega s_{\max}$$

$$I = \phi / A = 1/2 \rho v (\omega s_{\max})^2 \quad \text{Intensity of sound wave}$$

$$I = \Delta P_{\max}^2 / 2 \rho v$$

$$\beta = 10 \log(I/I_o) \quad \text{Decibals}$$

$$f' = \left( \frac{v \pm v_o}{v \mp v_s} \right) f \quad \text{Doppler effect}$$

+v<sub>O</sub> and -v<sub>S</sub> is toward is increase in f

-v<sub>O</sub> and +v<sub>S</sub> is away is decrease in f

$$y = 2A \cos(\phi/2) \sin(kx - \omega t + \phi/2) \quad \text{Resultant of 2}$$

$$\Delta r = \phi \lambda / 2\pi \quad \text{Relation between path diff and phase}$$

$$y = (2A \sin kx) \cos \omega t \quad \text{standing wave}$$

$$f_b = |f_1 - f_2| \quad \text{Beat frequency}$$

$$\alpha = \Delta L / L_i / \Delta T \quad \text{average coefficient of lin. Expans}$$

$$W = \int P dV$$

$$\Delta E_{\text{int}} = Q - W$$

$$W = nRT \ln(V_f / V_i) \quad \text{work done ideal gas isothermal}$$

$$\phi = kA |dT/dx| \quad \text{Thermal conduction}$$

$$\phi = \sigma A e T^4 \quad \text{Radiation}$$

$$PV^{C_p/C_v \text{ or } \gamma} = \text{constant}$$

$$e = 1 - Q_c / Q_h \text{ thermal efficiency}$$

$$e_c = 1 - T_c / T_h \text{ thermal of Carnot Engine}$$

$$q = mc\Delta T$$

$$q = mL_{\text{heat}}$$

$$v = \sqrt{\frac{3k_b T}{m}} = \sqrt{\frac{3RT}{M}}$$

$$K_{\text{av}} = 3/2 k_b T$$

$$Q = nC_v \Delta T$$

$$Q = nC_L \Delta T$$

$$\mathbf{E} = \mathbf{F}_e / q_0$$

$$\mathbf{F}_E = kq_1 q_2 / r^2$$

$$\mathbf{E}_o = kq_o / r^2$$

$$C = Q / \Delta V$$

$$U = kq_1 q_2 / r = q_{\text{test}} E_o r_{\text{ot}} \text{ (like } mgh) = q_{\text{test}} V = -W$$

$$V_o = kq_o / r = U / q_{\text{test}} = E_o r$$

$$E_x = -dV / dx \quad E_r = -dV / dr$$

$$\Delta V = \Delta U / q_{\text{test}} = -\int_{\infty}^0 E ds \text{ for uniform field} = -Ed$$

$$\Delta U / \Delta t = \Delta Q \Delta V / \Delta t = I \Delta V = \wp$$

$$\wp = IV = I^2 R = \Delta V^2 / R = \text{Watt}$$

$$\Phi_E = \int_{\text{surface}} \mathbf{E} \cdot d\mathbf{A} = q_{\text{in}} / \epsilon_0 \text{ (for closed surfaces)}$$

$$2k_e \lambda / r \quad \text{for linear}$$

$$\sigma / 2 \epsilon_0 \quad \text{for surface, just outside, no 2}$$

$$k_e Q / r^2 \quad \text{for outside hollow conducting sphere}$$

$$k_e Q / r^2 \quad \text{for uniform insulator sphere outside}$$

$k_e Qr / R^3$  for uniform insulator sphere inside

$$\Delta V = \Delta U / q = -\int \mathbf{E} \cdot d\mathbf{s} = -Ed \text{ in uniform field}$$

$$\boldsymbol{\tau} = \mathbf{p} \times \mathbf{E}$$

$$U = -\mathbf{p} \cdot \mathbf{E}$$

$$I = dQ / dt$$

$$J(\text{current density}) = I / A = nqv_d = A / m^2 \times$$

$$R = \Delta V / I = \rho \ell / A$$

$$\mathbf{F}_B = I\mathbf{L} \times \mathbf{B}$$

$$\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B} \quad \mu = IA = I\pi r^2 = 1/2 evr = (e/2m_e)L = \hbar\sqrt{2}(e/2m_e)$$

$$U = -\boldsymbol{\mu} \cdot \mathbf{B}$$

$$d\mathbf{B} = \frac{\mu_0 I ds \times \hat{\mathbf{r}}}{4\pi r^2}$$

$$\frac{F_B}{\ell} = \frac{\mu_0 I_1 I_2}{2\pi a}$$

$$\oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 I$$

$$\Phi_B = \int \mathbf{B} \cdot d\mathbf{A}$$